

## THE MODEL OF MEASURING WATER ACTIVITY IN FOOD PRODUCTS

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**SUMMARY:** One of the most important parameters of food products is the index "water activity". However, most of methods used for measuring  $A_w$  are characterised with substantial shortcoming. It is a large duration of measuring. That is why modelling the process of measuring  $A_w$  enabling to evaluate the influence of different factors on dynamical characteristics of devices is the essential stage of improving methods and technical facilities of measuring  $A_w$ .

**INTRODUCTION:** Consumer and technological properties of meat products are predetermined to a large extent by moisture content. But not so much total moisture content as that in forms and binding power is of interest. At present the index "water activity" ( $A_w$ ) has been finding increasingly growing use for evaluating binding power in food products. Microorganisms vital activity and kinetics of bio- and physical - chemical processes responsible for undesirable changes of food products quality depend on the  $A_w$  value (Troller and Christian, 1978; Scott, 1957; Labuza, 1977). At the same time water activity determines the nature of a number of its heat-mass-exchange processes (drying, diffusion, osmosis, sorption etc.) due to its thermodynamical nature. To measure  $A_w$  hygrometrical methods consisting in determining relative humidity of gaseous medium in the closed volume being in hygrothermal balance with the studied product are practised on a largest scale. Hygrometers of various types adapted for these purposes by means of applying special measuring chambers are widely used (Rodel, 1979; Von Elbe, 1986). The greatest disadvantage limiting the use of this index both in research and directly in production is a large duration of measuring  $A_w$  by this and other methods (as a rule, 2 - 3 hours). At the same time the authors of this work do not know the attempts of developing mathematical models of water activity measuring processes including devices of hygrometrical type, the use of which, to our opinion, will make it possible to make the analysis of factors influencing the duration of measuring and to outline the ways of its reduction.

**MATERIALS and METHODS:** Cooked doctor sausage (moisture 65 %) and fresh smoked special sausage (moisture 25 %) were taken as samples. Investigation was carried out with the help of VOLNA - 5 hygrometer (Angarsk EDBA) with digital indication, two types of standard humidity indicator (with mechanical filter and without it) being used. Indicators were placed in measuring chambers with volumes of 8 ml and 28 ml. Transfer characteristic was determined by recording hygrometer readings on a diagram band. Uneven agitation was provided by connecting the measuring chamber with humidity indicator to the container with the studied sample. During this process the chamber with the indicator was held in the medium with relative humidity of 30 %.

**RESULTS and DISCUSSION:** Measuring  $A_w$  by devices of hygrometrical type is based on non-stationary heat-mass-exchange. During this process, first of all, moisture exchange of a food product surface with air in the closed volume takes place. Secondly, there occurs aqueous vapour diffusion in air medium of the measuring chamber. Thirdly, adsorption of moisture from air by moisture sensitive element goes on. Fourthly, internal heat-mass-exchange between a surface and inner layers of a sample also takes place. To study the process of measuring  $A_w$  by hygrometrical method we have developed a dynamical mathematical model which is based on the following assumptions:

- the inertial moisture transfer is negligibly small in comparison with moisture return from the surface of a sample;
- the time of balance establishment between the boundary layer and the surface of a sample is not taken into account;

- temperature ( $\theta$ ), pressure, rate of moisture diffusion in air as well as mass-exchange characteristics and water activity of a sample in the process of measuring are constant.

The intensity of moisture exchange with air in the volume  $V$  of the chamber with assumptions mentioned above practically doesn't depend only on the gradient of relative humidity on the surface of a boundary layer.

$$\Delta RH = f(RH_b - RH_c), \quad (1)$$

where  $RH_b$  and  $RH_c$  are relative humidity of a boundary layer and in the chamber. While measuring  $A_w$  at the initial moment of time, in the chamber there appears the gradient of moisture which gradually lowers, relative humidity in the boundary layer is proportional to this gradient:

$$RH_b = K_1 (A_w - RH_c - RH_i) = K_1 \Delta RH \quad (2)$$

where  $RH_i$  is the initial relative humidity in the chamber. Thus, transfer function  $W_1(S)$  is approximated by the proportional link

$$W_1(S) = K_1 \quad (3)$$

As it was determined before the rate of the boundary layer moisture exchange with the air of the chamber is considerably lower than the rate of its moisture exchange with the sample and is proportional to the coefficient of aqueous vapour diffusion in the air

$$dRH/dt = K_2 RH_c \quad (4)$$

Hence, transfer function  $W_2(S)$  describes the proportional link

$$W_2(S) = K_2, \quad K_1 \cdot K_2 = F \cdot K \quad (5)$$

Relative humidity in the chamber is proportional to the amount of moisture accumulated in its volume  $V$  during the process  $t$

$$RH_c = K_3 \int_0^t RH_c(t) dt, \quad K_3 = (R \cdot \theta) / V \quad (6)$$

where  $R$  is the universal gas constant. Consequently, transfer function  $W_3(S)$  describes the integrating link

$$W_3(S) = K_3 / S \quad (7)$$

In the case of humidity indicator being mounted at some distance from the sample surface, presence of mechanical and other filters, transfer function  $W_4(S)$  must approximate the link of lag

$$W_4(S) = \exp(-st_1) \quad (8)$$

where  $t_1$  - is the time of pure transport lag, sec. Transfer function  $W_4(S)$  reflects dynamical properties of moisture sensitive element of indicator and describes aperiodical link of the first order

$$W_5(S) = K_5 / (T_5 S + 1) \quad (9)$$

The structural scheme of the process corresponding to the developed model is presented on Fig. 1. Transfer function of the whole process along the canal " $A_w - RHe$ " has the form

$$W_e(S) = \frac{W_1(S) \cdot W_2(S) \cdot W_3(S)}{1 + W_1(S) \cdot W_2(S) \cdot W_3(S)} \cdot W_4(S) \cdot W_5(S) \quad (10)$$

After transformations the equation of the whole process has the form

$$[T T_5 S^2 + (T + T_5)S + 1] RHe(t) = K_5 (A_w - RH_i) \exp(-st_1) \quad (11)$$

where  $T = V / (R \cdot \theta \cdot F \cdot K) = 1 / (K_1 K_2 K_3)$

As the incoming ( $A_w$ ) and outgoing ( $RHe$ ) parameters are measured in the same units, amplification constant  $K_5 = 1$ . Having designated  $T_1^2 = T_5 T$ ;  $T_2 = T_5 + T$ , we write the equation in new designations

$$(T_1^2 S^2 + T_2 S + 1) RHe(t) = (A_w - RH_i) \exp(-st_1) \quad (12)$$

Fig. 2 shows a typical transfer characteristic of the process of measuring  $A_w$  in the conditions of hygrometrical type. As a result of processing experimental data, this process may be approximated in the common case by the differential equation of the second order.

Constants  $T_1$  and  $T_2$  were determined graphically by traditional methods.

Test of model for adequacy by means of a computer showed a good coincidence with experimental

data (the divergence is not more than 5 %) while substituting parameters obtained.

**CONCLUSIONS:** Analysis of the model and experimental results obtained makes it possible to conclude that the lag affects only when using measuring chambers of a large volume and moisture indicators with low dynamical characteristics (e.g. filters). The time constant reduces while reducing the chamber volume and enlarging the effective evaporation area of a sample. During this process the time constant of the chamber with a sample (T2) is not substantially changed when investigating various food products in the same conditions.

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Conditions of carrying out the experiment and the model s parameters

Food product	Chamber volume	Filter	Water activity	Model s parameters (sec.)				
	V, ml	availabi-lity		Aw	t1	T1	T2	T3
Cooked sausage	8,0	yes	0,965	0	18,5	71,0	70,7	0,3
	8,0	no	0,965	0	0	54,0	54,0	0,3
	28,0	yes	0,965	5,0	30,8	110,0	109,7	0,3
	28,0	no	0,965	0	19,0	57,0	56,7	0,3
Fresh smoked sausage	8,0	yes	0,852	0	21,6	93,0	92,7	0,3
	8,0	no	0,852	0	0	75,0	75,0	0,3
	28,0	yes	0,852	9,2	41,1	153,0	152,7	0,3
	28,0	no	0,852	0	34,7	124,0	123,7	0,3

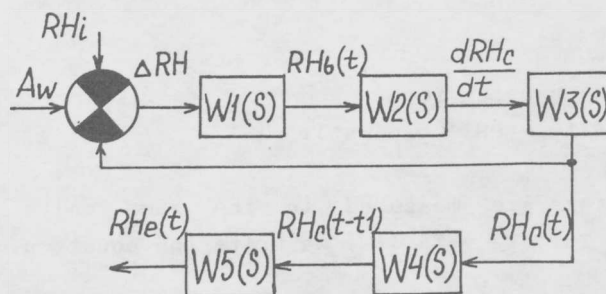


Fig.1. Structural scheme of the process of measuring Aw by devices of hygrometrical type

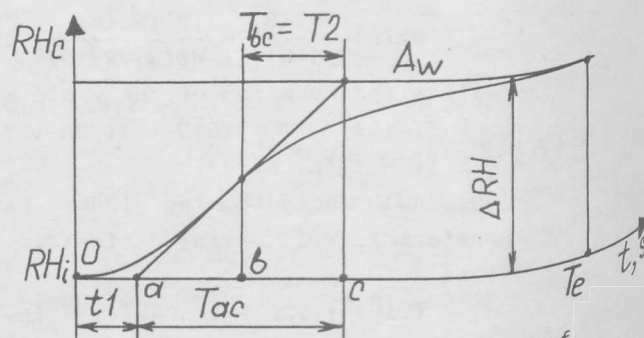


Fig.2. Typical surge characteristic of the process of measuring Aw by devices of hygrometrical type